

## Grade 6

### Concepts and Procedures

#### Ratios and Proportional Relationships

<p>RANGE ALD Target A: Understand ratio concepts and use ratio reasoning to solve problems.</p>	<p>Level 1 students should be able to describe a ratio relationship between two whole number quantities, find missing values in tables that display a proportional relationship, and plot the pairs of values from a table on a coordinate plane. They should be able to find a percent as a rate per hundred and convert measurement units.</p>	<p>Level 2 students should be able to demonstrate understanding of the concept of unit rate and solve one-step problems requiring ratio reasoning in a familiar context.</p>	<p>Level 3 students should be able to use ratio reasoning to solve and demonstrate understanding of the concept of unit rates in unfamiliar multistep problems, including instances of unit pricing and constant speed, and solve percent problems by finding the whole, given a part and the percent. They should be able to describe a ratio relationship between any two number quantities.</p>	<p>Level 4 students should be able to solve unfamiliar multistep problems by finding the whole, given a part and the percent; explain ratio relationships between any two number quantities; and identify relationships between models or representations.</p>
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#### The Number System

<p>RANGE ALD Target B: Apply and extend previous understandings of multiplication and division to divide fractions by fractions.</p>	<p>Level 1 students should be able to apply and extend previous understandings of multiplication and division to multiply a fraction by a fraction, divide a fraction between 0 and 1 by a whole number, and connect to a visual model. They should be able to understand the effect that a fraction greater than or less than 1 has on a whole number when multiplied and use or create visual models when multiplying a whole number by a fraction between 0 and 1.</p>	<p>Level 2 students should be able to apply and extend previous understandings of multiplication and division to divide a whole number by a fraction, divide a mixed number by a whole number, and connect to a visual model.</p>	<p>Level 3 students should be able to apply and extend previous understandings of multiplication and division to divide a fraction by a fraction and be able to connect to a visual model.</p>	<p>Level 4 students should be able to apply and extend previous understandings of multiplication and division to solve real-world and mathematical problems</p>
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<p>RANGE ALD Target C: Compute fluently with multidigit numbers and find common factors and multiples.</p>	<p>Level 1 students should be able to add, subtract, and multiply multidigit whole numbers and decimals to hundredths. They should be able to use the distributive property to express the sum of two whole numbers with a common factor.</p>	<p>Level 2 students should be able to divide multidigit whole numbers and add, subtract, and multiply multidigit decimal numbers. They should be able to find common factors of two numbers less than or equal to 100 and multiples of two numbers less than or equal to 12.</p>	<p>Level 3 students should be able to fluently divide multidigit numbers and add, subtract, multiply, and divide multidigit decimal numbers. Students should be able to express the remainder as a whole number, decimal, or simplified fraction. They should be able to find the greatest common factor of two numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12.</p>	<p>Level 4 students should be able to make generalizations regarding multiples and factors of sets of numbers (e.g., state that a particular set of numbers is relatively prime).</p>
<p>RANGE ALD Target D: Apply and extend previous understandings of numbers to the system of rational numbers.</p>	<p>Level 1 students should be able to place all integers on a number line and integer pairs on a coordinate plane with one-unit increments on both axes.</p>	<p>Level 2 students should be able to apply and extend previous understandings of whole numbers to order rational numbers and interpret statements of their order in the context of a situation. They should be able to place all rational numbers on a number line and integer pairs on a coordinate plane with various axis increments. They should be able to relate changes in sign to placements on opposite sides of the number line and understand the absolute value of a number as its distance from zero on a number line.</p>	<p>Level 3 students should be able to apply and extend previous understandings of numbers to relate statements of inequality to relative positions on a number line, place points with rational coordinates on a coordinate plane, and solve problems involving the distance between points when the points share a coordinate. They should be able to demonstrate understanding of absolute value and ordering by using number lines and models and relating reflection across axes to changes in sign.</p>	<p>No Descriptor</p>

<p>RANGE ALD Target E: Apply and extend previous understandings of arithmetic to algebraic expressions.</p>	<p>Level 1 students should be able to evaluate numerical expressions without exponents; write one- or two-step numerical expressions; and identify parts of an expression, using terms (e.g., coefficient, term, sum, product, difference, quotient, factor).</p>	<p>Level 2 students should be able to evaluate numerical expressions with whole-number exponents that do not need to be distributed across a set of parentheses. They should be able to apply and extend previous understandings of arithmetic to evaluate expressions with variables that do not contain exponents. They should be able to write one- and two-step algebraic expressions that introduce a variable and identify equivalent expressions.</p>	<p>Level 3 students should be able to write and evaluate numerical expressions with whole-number exponents and expressions from formulas in real-world problems, and they should be able to apply and extend previous understandings of arithmetic to evaluate expressions with variables that include whole-number exponents. They should be able to apply properties of operations to generate equivalent expressions.</p>	<p>Level 4 students should be able to apply the understanding of the properties of operations and use the properties to show why two expressions are equivalent.</p>
<p>RANGE ALD Target F: Reason about and solve one-variable equations and inequalities.</p>	<p>Level 1 students should be able to use substitution to determine when a given number makes an equation or inequality true.</p>	<p>Level 2 students should be able to solve one-variable equations and inequalities of the form <math>x + p = \frac{a}{b}q</math> or <math>px = \frac{a}{b}q</math>, where <math>p</math> and <math>q</math> are nonnegative rational numbers. They should be able to identify and use variables when solving equations.</p>	<p>Level 3 students should be able to write one-variable equations and inequalities of the form <math>x + p = \frac{a}{b}q</math> or <math>px = \frac{a}{b}q</math>, where <math>p</math> and <math>q</math> are nonnegative rational numbers. They should be able to solve equations and inequalities by writing and graphing their solutions on a number line.</p>	<p>Level 4 students should be able to write and solve equations and inequalities of the form <math>x + p = \frac{a}{b}q</math> or <math>px = \frac{a}{b}q</math>, where <math>p</math> and <math>q</math> are rational numbers. They should be able to write and graph solutions on the number line.</p>
<p>RANGE ALD Target G: Represent and analyze quantitative relationships between dependent and independent variables.</p>	<p>Level 1 students should be able to identify a table that represents a relationship between two variables of the forms <math>y = kx</math> and <math>y = x \pm c</math> with rational numbers and plot points corresponding to equations on coordinate planes.</p>	<p>Level 2 students should be able to use variables to represent and analyze two quantities that change in relationship to each other of the form <math>y = kx</math> or <math>y = x \pm c</math> with rational numbers; identify and create an equation that expresses one quantity in terms of another; and use graphs and tables to represent the relationship.</p>	<p>Level 3 students should be able to use graphs, tables, or context to analyze the relationship between dependent and independent variables and relate them to a linear equation.</p>	<p>Level 4 students should be able to use graphs, tables, or context to analyze nonlinear polynomial relationships between dependent and independent variables and relate them to nonlinear polynomial equations.</p>

## Geometry

<p>RANGE ALD Target H: Solve real-world and mathematical problems involving area, surface area, and volume.</p>	<p>Level 1 students should be able to find areas of right triangles; draw polygons with positive coordinates on a grid with a scale in one-unit increments, given nonnegative integer-valued coordinates for the vertices; and find the volume of right rectangular prisms with one side expressed as a fraction or a mixed number in halves or fourths.</p>	<p>Level 2 students should be able to find areas of special quadrilaterals and triangles; draw polygons in the four-quadrant coordinate plane with scales in one-unit increments, given integer-valued coordinates for the vertices; and find the volume of right rectangular prisms with one side expressed as a fraction or a mixed number.</p>	<p>Level 3 students should be able to solve problems that involve finding areas of polygons and special quadrilaterals and triangles and find the volume of right rectangular prisms with all sides expressed as a positive rational number. They should be able to solve problems by drawing polygons in the four-quadrant coordinate and determine the length of a side joining the coordinates of vertices with the same first or the same second coordinate.</p>	<p>Level 4 students should be able to solve problems by finding surface areas of three-dimensional shapes composed of rectangles and triangles. They should be able to find the volume of a compound figure composed of right rectangular prisms to solve problems.</p>
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## Statistics and Probability

<p>RANGE ALD Target I: Develop understanding of statistical variability.</p>	<p>Level 1 students should be able to identify questions that lead to variable responses posed in familiar contexts and recognize that such questions are statistical questions.</p>	<p>Level 2 students should be able to recognize that questions that lead to variable responses are statistical questions and vice versa, and they should relate the concept of varying responses to the notion of a range of possible responses. They should demonstrate an understanding that the responses to a statistical question will have a representative center and a given set of numerical data. They should be able to identify a reasonable measure of central tendency with respect to a familiar context.</p>	<p>Level 3 students should be able to pose statistical questions and demonstrate understanding that the responses to a statistical question have a distribution described by its center, spread, and overall shape. They should demonstrate understanding that a measure of center summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number. They should be able to identify a reasonable center and spread with respect to a familiar context.</p>	<p>Level 4 students should be able to justify the reasonableness of their identified center and spread with respect to an unfamiliar context. They should be able to create or complete a data set with given measures (e.g., mean, median, mode, interquartile range).</p>
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<p>RANGE ALD Target J: Summarize and describe distributions.</p>	<p>Level 1 students should be able to summarize or display numerical data on a number line, in dot plots, and in histograms; find the median of an odd number of data points; and find the mean when data points are nonnegative integers.</p>	<p>Level 2 students should be able to calculate measures of center, demonstrate understanding that measures of center can be different or the same, and use the measure of center to summarize data with respect to the context.</p>	<p>Level 3 students should be able to summarize or display data in box plots and find the interquartile range. They should be able to use the interquartile range along with the measures of center to describe overall patterns in a data distribution, such as symmetry, clusters, and any striking deviations. They should be able to examine a data set in context and explain the measures of center, as it relates to the data.</p>	<p>Level 4 students should be able to relate the choice of measures of center and variability to the shape of the data distribution in context of the data; find mean absolute deviation and identify outliers with reference to the context of the situation; and predict effects on the measures of center, given a change in data points.</p>
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